### **Graph Theory in Operational Research**

#### Application exercise 2 Water supply

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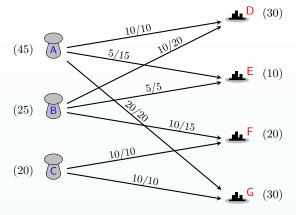


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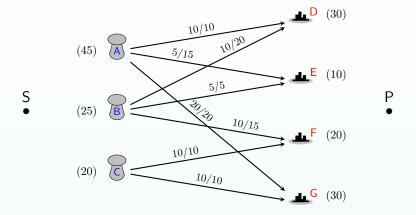
# Water supply

- 4 villages are supplied with water by 3 water towers
- Each water tower has a maximum rate of flow expressed in L/s
- Each village expresses preferential needs in L/s
- Various pipes exist between water towers and villages, whose current capacities and uses are known

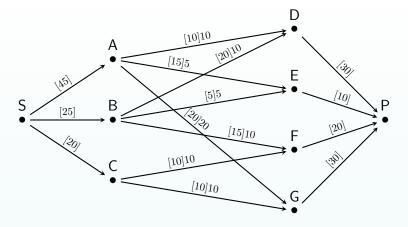
### Water supply



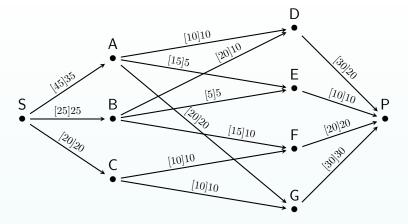
- Modelize the transport network. What is the value of the flow?
- 2 Determine the maximum flow.
- Sometimes of the possible additions to meet the minimum requirements.



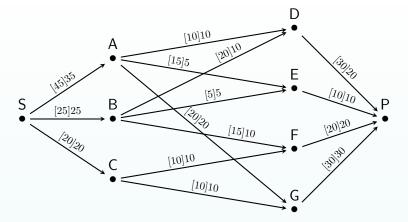
Adding virtuals source and sink



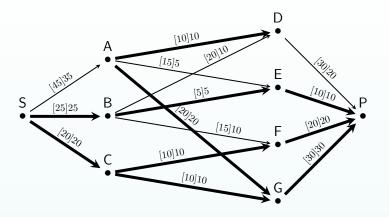
• Capacities related to the problem values

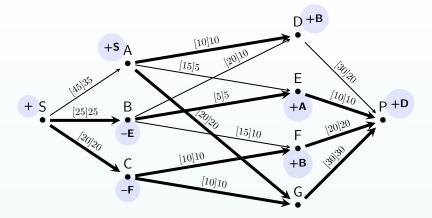


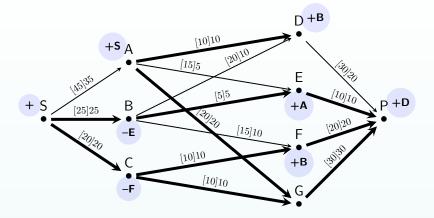
• Flow calculated by Kirchhoff's law



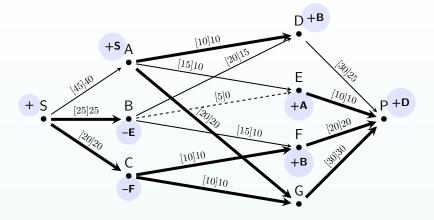
- Flow calculated by Kirchhoff's law
- $\varphi = 80$



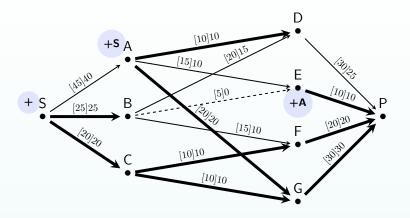




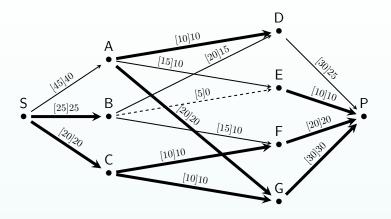
 $\bullet \ \ {\rm Augmenting \ path} \ (S,A,E,B,D,P) \\$ 



 $\bullet$  Augmenting path (S,A,E,B,D,P) :  $\delta=5$ 

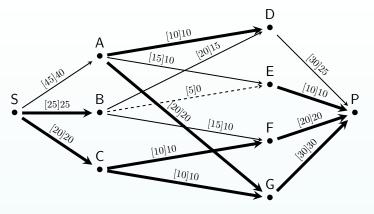


No more augmenting path



 $\bullet$  Maximum flow:  $\varphi=85$ 

### Minimum possible additions



Adding an arc with a capacity of 5 on one of the three paths:

- $\bullet$  (A, B)
- $\bullet$  (A, D)
- $\bullet$  (E,D)

### Conclusions

- The initial flow is  $\varphi = 80$
- The maximum flow is  $\varphi=85$
- The validation of preferential needs can't be achieved without changing the network
- 3 optimal amendments are identified

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http://www.damien-leprovost.fr/enseignements/graphs.2015.ex2.pdf